Preference of subpicosecond laser pulses for terahertz wave generation from liquids

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Abstract. Terahertz (THz) wave generation from laser-induced air plasma generally requires a short temporal laser pulse. In contrast, it was observed that THz radiation from ionized liquid water prefers a longer pulse, wherein the mechanism remains unclear. We attribute the preference for longer pulse duration to the process of ionization and plasma formation in water, which is supported by a numerical simulation result showing that the highest electron density is achieved with a subpicosecond pulse. The explanation is further verified by the coincidence of our experimental result and simulation when the thickness of the water is varied. Other liquids are also tested to assure the preference for such a pulse is not exclusive to water.

Keywords: terahertz wave generation from liquids; laser-induced ionization; plasma.

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1 Introduction

Tremendous interest in terahertz (THz) science and technology has arisen, due to wide applications in nondestructive evaluation,1,2 the pharmaceutical industry,3,4 nonlinear interaction,5,6 and electron acceleration.7,8 With successive development, numerous groups have demonstrated THz wave generation9 from solids,10–19 gases,20 and plasmas.21,22 Recently, THz wave generation from liquids under the excitation of intense laser pulses has been reported as well.23–27

The generation process of THz radiation from liquids23,25,26 resembles that from gases, due to the fact that laser-induced ionization plays a significant role in both generation processes. In both cases, a model based on a ponderomotive force-induced dipole has been commonly used for the one-color excitation scheme,25,27–29 and a transient current model was successfully applied for the two-color excitation scheme.26,30–32 Remarkably, one distinction between the two cases is that the dependence of THz radiation on the optical pulse duration is very different: THz radiation from gases favors a short optical pulse, whereas a longer pulse offers stronger THz emission in liquids. The phenomenon was experimentally observed while a physical explanation was still absent.23 Moreover, it was observed that only a 10-times enhanced THz field was obtained when an asymmetric excitation was applied to replace the one-color excitation scheme in the liquid.26 Compared with the many orders of magnitude improvement in the gas,22 this lower enhancement may be caused by the limitation in optical pulse duration. Studying the effect of pulse duration on the THz radiation is crucial to understand the involved physics and therefore provides insights to boost THz emission from liquids.

2 Experimental Setup

For the experimental study, liquid lines are introduced as the THz sources.23 Figure 1(a) shows a photo of a 260-μm diameter water line, which is produced by a 260-μm inner diameter syringe needle (BSTEAN™). A Masterflex L/S digital pump from Cole-Parmer® is used to drive the liquid. We define that the liquid line flows along the y direction. A femtosecond amplified laser (Ti:sapphire) with a central wavelength of 800 nm and a repetition rate of 1 kHz is used for the excitation. The flow velocity of the liquid is controlled to be 7 m/s. In this case, each laser pulse will interact with a fresh liquid spot. A horizontally polarized laser beam with 0.4 mJ pulse energy propagating along the z direction is focused into the liquid by a 2-in. effective focal length lens (F/4) to generate THz waves. A high-resistivity silicon wafer acts as a filter to block the residual laser beam while allowing the THz beam to pass through. The THz electric field is measured by a 2-mm thick, (110)-cut ZnTe crystal placed in the direction of laser propagation through electro-optic sampling.33
3 Results of Experiments and Simulations

3.1 THz Fields from a Water Line

Figure 1(b) shows the peak values of THz fields when the 260-μm diameter water line is scanned along the $x$ direction across the laser focal point. For $x = \pm 150 \mu m$, the signal from water is also recorded even though the laser focal point is in the air. The ionization in the water still occurs when the focus is not far away from the water surface. A weak THz signal is detected at $x = 0 \mu m$, which is represented as the black dot in the middle. This coincides with the case of a water film with a normally incident laser beam. In contrast, the THz signal becomes significant when the water line is shifted away from the zero position in the $x$ direction. The THz field is maximized at $x = \pm 90 \mu m$, which is caused by the ponderomotive force-induced current with the symmetry broken around the interface. The value of the THz peak field changes in sign from negative to positive. If two points are symmetric about 0, their absolute values of THz peak field are identical. The waveforms of the THz signals at $x = \pm 90 \mu m$ are shown in Fig. 1(c). Clearly, the THz waveforms flip over when their $x$ positions are mirrored with respect to the zero position. The results shown in Figs. 1(b) and 1(c) can also be explained by the dipole model mirrored $x$ position leads to an opposite projected direction of the dipole in water, resulting in an inverted THz waveform. For $x = 0 \mu m$, the dipole in water is oriented along the direction of laser propagation contributing to weak THz radiation in the $z$ direction. Thus a tilted dipole realized by a shift of the water line in the $x$ direction is essential to obtain the strongest THz signal in the direction of laser propagation. In the following sections, $x = 90 \mu m$ will be used for the experiment.

3.2 Optimal Pulse Duration

To explore the dependence of THz radiation on the optical pulse duration, laser pulses are stretched in time by adjusting the compressor stage integrated within the laser to achieve various pulse durations while the laser pulse energy is kept the same. The corresponding THz energy from a 210-μm diameter water line is recorded and shown as the black dot in Fig. 2. Unlike the case of air, a subpicosecond pulse (345 fs) is required for the optimization of THz radiation from liquid water. In this paper, subpicosecond is defined as 200 to 800 fs.

The result of the optimal pulse duration can be understood from the interaction between the laser field $E(z, t)$ and the water, which is described by the following wave equation:

$$\frac{\partial E}{\partial z} = \frac{i}{2n\kappa_0} \nabla^2 E + ik_0n_2|E|^2E - \frac{i\beta_2}{2} \frac{\partial^2 E}{\partial t^2} - \frac{\sigma}{2}(1 + i\omega\tau)\rho E - \beta^{(\text{eff})}|E|^{2K-2}E, \quad (1)$$

where the terms on the right-hand side represent transverse beam diffraction, self-focusing (SF), group velocity dispersion (GVD), plasma absorption and defocusing, and multiphoton absorption, respectively. Here $n$ is the refractive index, $\kappa_0$ is the wave vector, $n_2$ is the nonlinear coefficient, $\beta_2 = \partial^2 k/\partial \omega^2$ represents GVD, $\sigma = (ke^2\tau/m\omega c_0)/(1 + \omega^2\tau^2)$ is the cross section for inverse Bremsstrahlung absorption, $\omega$ is the optical frequency, $\tau$ is the electron collision time, $\rho$ is the electron density, and $\beta^{(\text{eff})}$ is the nonlinear coefficient for $K$-photon absorption.

Electrons are produced by intense laser pulses through multiphoton ionization (MPI)/tunneling ionization (TI) and cascade ionization at the focus. MPI/TI directly ionizes water

Fig. 1 (a) Photograph of the water line produced by a syringe needle in a side view. The diameter of the water line is 260 μm. Its flowing velocity is 7 m/s along the y direction. The laser beam propagates in the z direction. The water line can be moved along the x direction by a translation stage. (b) THz peak fields with different $x$ positions when the 260-μm diameter water line is crossing the laser focal point along the x direction. (c) THz waveforms at $x = \pm 90 \mu m$ in (b).

Fig. 2 Effect of optical pulse duration on THz energy and peak electron density for a 210-μm water line. The black dots are the experimental data for THz energy. The red curve is the simulation data for peak electron density.
molecules while cascade ionization desires the presence of free electrons for initiation. These free electrons come from the background electrons and MPI/TI. In our experimental condition, the laser intensity at the focus is at the level of $10^{15}$ W/cm$^2$. The Keldysh parameter $\gamma = 0.23$ is obtained when water is treated as an amorphous semiconductor with a bandgap of $U = 6.5$ eV,$^{36,41-43}$ indicating that TI dominates over MPI in our case.$^{46,44}$ Thus the last term of Eq. (1) needs to be modified to $rac{\eta_I (\rho_{\text{water}} - \rho)}{\tau^{\eta}} E$ when TI dominates.$^{45}$ The electron density $\rho(z, t)$ satisfies the rate equation:

$$\frac{\partial \rho}{\partial t} = \eta_I (\rho_{\text{water}} - \rho) + \eta_{\text{cas}} - \eta_{\text{diff}} - \eta_{\text{rec}} \rho^2. \quad (2)$$

The first two terms on the right-hand side correspond to the generation of electrons from TI and cascade ionization. The other two terms describe the loss of electrons from diffusion and recombination. $\rho_{\text{water}}$ is the molecular density of water. The laser pulse is considered to have a Gaussian profile with its intensity as follows:

$$I(t) = 0.94 \frac{E_p}{\tau_p} \exp \left[ -4 \ln 2 \left( \frac{t}{\tau_p} \right)^2 \right] / (0.5\pi\omega_0^2), \quad (3)$$

where $E_p$ is the laser pulse energy, $\tau_p$ is the laser pulse duration, and $\omega_0$ is the beam waist at the focus.

It is worth underlining that each cascade process needs an ionization time $\tau_{\text{ion}}$ to perform. Thus one seed electron cannot produce more than $2\tau_{\text{ion}}/\tau_p$ electrons through the cascade process, regardless of the laser intensity. Comparing with the increase of electrons due to TI, the exponential boost caused by cascade ionization makes it the dominating ionization process in water when $\tau_p$ is above 40 fs.$^{37}$ Therefore, a longer pulse duration that allows for more cascades taking place benefits plasma formation through the exponential increase from cascade ionization. Even though the majority of electrons are provided by cascade ionization, TI is still quite important because it provides most of the electrons to initiate the cascade process, especially in pure water. Since TI highly depends on laser intensity and laser intensity is inversely proportional to $\tau_p$, if the laser pulse energy $E_p$ is fixed [see Eq. (3)], generated electron density will start to decrease if $\tau_p$ raises too much. Considering the fact that higher electron density contributes to more THz radiation, the trade-off between the two effects can lead to the preference for a subpicosecond pulse.

Simulations are carried out to verify the theoretical analysis. The laser wavelength and pulse energy are set to match the values in the experiment. In our experiment, a strong external focusing is used, where the SF and the geometrical focusing become indistinguishable.$^{46}$ Thus the term of SF is not included in the simulation. We also assume that the impact of GVD is insignificant because the plasma length of our interest is short ($\sim 200 \mu$m). The electron collision time $\tau = 1$ fs and the cascade ionization time $\tau_{\text{ion}} = 5$ fs are applied.$^{37}$ Since femtosecond and subpicosecond laser pulses are used in the experiment, contribution from diffusion is justifiably neglected.$^{37,43}$ The TI rate $\eta_I(t)$ can be acquired by the ADK model.$^{48}$ The cascade ionization rate $\eta_{\text{cas}}$ is calculated as in Ref. 37. The recombination rate $\eta_{\text{rec}}$ is taken to be $2 \times 10^{-9}$ cm$^3$/s.$^{37,49}$ The molecular density of water $\rho_{\text{water}}$ is $3.34 \times 10^{22}$ cm$^{-3}$.$^{36}$ The initial electron density is chosen to be $\rho_0 = 10^{10}$ cm$^{-3}$, which will hardly impact on the evolution of electron density even if $\rho_0$ is changed over several orders of magnitude.$^{34,35}$ By numerically solving the coupled Eqs. (1) and (2) with different values of pulse duration, the evolution of electron density $\rho(z, t)$ that corresponds to different $\tau_p$ is obtained. Consequently, the peak electron density versus $\tau_p$ is achieved and plotted (see the red curve in Fig. 2). As expected, a subpicosecond pulse is a requisite for the highest peak electron density.

For further verification, the diameter of the water line $d$ is chosen as a variable to see how the optimal pulse duration changes with the water line diameter in the experiment and simulation. Experimentally, seven individual syringe needles with different inner diameters are used to produce water lines with diameters varying from tens of microns to half a millimeter. The optimal pulse duration for the THz energy from each water line is recorded and shown as the red dot in Fig. 3. The optimal pulse duration gradually changes from 257 to 513 fs when $d$ increases from 90 to 510 $\mu$m. In the simulation, the evolution of electron density that corresponds to different $\tau_p$ is achieved. Then the peak electron density is integrated over $z$ within the whole range of the water line that is determined by the diameter $d$. Thus the optimal pulse duration for the highest electron density that corresponds to the different diameter of the water line is obtained (see the blue squares in Fig. 3). To make the result clear to see, only a few points in a similar range of the experiment are shown. The coincidence of the experimental result and the simulation supports our model and explanation.

### 3.3 Applicability to Other Liquids

To confirm that the preference for a subpicosecond laser pulse is not exclusive to water, other liquids such as $\alpha$-pinene, p-xylene, and ethanol are experimentally tested as well. It is noticeable that there are some material-related parameters involved in the simulations, such as refractive index, nonlinear coefficient, ionization energy, ionization time, and molecular density. These parameters may take effect as well. In our experiment, all these liquids exhibit an optimal pulse duration around 345 fs when their diameters have the same value of 210 $\mu$m. Therefore, these parameters do not substantially affect the optimal pulse duration. However, they still demonstrate the influence on the THz radiation. Here we use $\alpha$-pinene as an example to show

**Fig. 3** Optimal optical pulse duration versus the diameter of the water line. The blue squares are simulations of optimal pulse duration aiming for highest electron density. The red dots are the experimental data obtained with strongest THz energy.
its comparison with water. Figure 4(a) shows the THz waveforms that are generated from a 210-μm diameter α-pinene and water line. The dash line in (b) is calculated by removing the absorption of α-pinene and adding the absorption of water to the black curve from 0.5 to 2.5 THz. Inset: measured results of refractive index n (dots) and field absorption coefficient α (circles) of α-pinene within 0.5 to 2.5 THz.

3.4 Discussion

We note that the subpicosecond optimal pulse duration for THz wave generation was also previously reported by Wang et al. [56]. The preference for longer pulses was attributed to the longer interaction time of the gas atoms with the laser. Even though the result has similarities to ours, they did study a different case, which is the two-color excitation scheme in gases, whereas our work focuses on the one-color case in liquids.

It also needs to be mentioned that the demonstration of preference for a subpicosecond optical pulse can also be used to explain the low enhancement of THz radiation under the two-color excitation. [27] The subpicosecond pulse is indispensable to achieve high electron density in the liquid, as we have just demonstrated. Nevertheless, a short pulse works much better for the second-harmonic generation from the fundamental beam. The discrepant demand regarding the pulse duration significantly limits the generation of THz waves under the two-color excitation. Considering that the THz field strength of 0.2 MV/cm from the water was claimed by Zhang et al. [27] under the one-color excitation, a very intense THz radiation could be expected if the requirements for pulse duration are satisfied under the two-color excitation. One possible solution is separately controlling the phase and polarization of the fundamental beam and the second-harmonic beam using a dichroic mirror. [37] Another dichroic mirror can be applied to combine the second-harmonic beam and the stretched fundamental beam. Such an arrangement assures that the plasma would be generated by a time-stretched pulse and that the second-harmonic component remains intense.

4 Conclusion

To summarize, the preference for a subpicosecond laser pulse for THz wave generation from liquids is understood from the process of laser-induced plasma formation based on our experimental results and simulations. On one hand, cascade ionization, the dominant ionization process leading to an exponential increase in the number of electrons, needs a long pulse duration. On the other hand, increasing the pulse duration sacrifices the increase in the number of electrons, needs a long pulse duration. The trade-off between the two effects results in an optimal pulse duration around the subpicosecond region. Unlike the speculation given in Ref. [23] where cascade ionization is the only reason for the preference, electron collision time and TI are demonstrated to be critical factors as well. Other liquids such as α-pinene, p-xylene, and ethanol are also tested to ensure that the preference for a subpicosecond pulse does not only occur in water. In addition to unveiling the influence of optical pulse duration on laser-induced plasma formation for THz radiation, our observations also contribute insight into the development of intense liquid THz sources.

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References


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