Design Description Document

Light Weight/Low Cost/High Powered Solar Concentrator

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Project Overview:

This optics senior design team is tasked with exceeding the performance of Professor Knox’s design by increasing the total concentrated power and efficiency of a solar concentrator.
Table of Contents

Background

Problem Statement

Requirements

Specifications

Optical Design Analysis

Mechanical Frame Concepts

  Concept Selection Matrix

Cost Analysis

Frame CAD for Fabrication

Product Requirement Document

System Flowchart

Appendix A: Optical System Design

Appendix B: Finite Element Modeling

Appendix C: Test Plan / Validation
## Revision History

<table>
<thead>
<tr>
<th>Rev</th>
<th>Description</th>
<th>Date</th>
<th>Authorization</th>
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<tbody>
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<td>A</td>
<td>Creation of the DDD</td>
<td>01/31/2016</td>
<td>MLD</td>
</tr>
<tr>
<td>B</td>
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</tr>
<tr>
<td>C</td>
<td>Revision after presentation.</td>
<td>02/15/2016</td>
<td>MLD</td>
</tr>
<tr>
<td>D</td>
<td>Revision for Midterm.</td>
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</tr>
<tr>
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</tr>
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Background
Professor Wayne Knox, our customer, built a solar concentrator in his garage using plywood, reflective Mylar, tape, and a vacuum cleaner. This concave mirror is able to burn lumber, cook burgers, and scorch asphalt in a matter of seconds. The optical engineering senior design team this year is tasked with pushing Knox’s design to the next level, increasing the total concentrated power and efficiency. The mechanical engineering senior design this year is tasked to design the system that will allow for increasing the total concentrated power and efficiency.

Figure 1: On left, Wayne Knox (our customer and competitor) takes a picture of his solar concentrator before a vacuum is applied. On right, the concentrator is able to ignite a block of wood.

Problem Statement
The goal of this project is to design a solar concentrator that has the capability of being scaled by the manufacturer and shipped to remote locations or developing countries. The design has to be optimized in weight, size, and optical power efficiency.

Product Requirement Document
See Final Solar PRD
**System Flowchart**

![System Flowchart Diagram]

Figure 2: The approach used in designing, building, testing and revising our project prototypes.

### Requirements

<table>
<thead>
<tr>
<th>Number</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>More efficient at collecting sunlight than Knox’s prototype.</td>
</tr>
<tr>
<td>2</td>
<td>Must be lighter than Knox’s prototype.</td>
</tr>
<tr>
<td>3</td>
<td>Before creating the vacuum the membrane should be flat, uniform, and not under tension.</td>
</tr>
<tr>
<td>4</td>
<td>Before creating the vacuum, the membrane should be over an open circular area to create the ideal reflective surface shape.</td>
</tr>
<tr>
<td>5</td>
<td>The vacuum method must be used to create a pressure differential that will create the curved reflective Mylar surface. This vacuum method may be a passive vacuum.</td>
</tr>
<tr>
<td>6</td>
<td>Must be shippable in a cardboard box.</td>
</tr>
<tr>
<td>7</td>
<td>The reflective Mylar must be replaceable.</td>
</tr>
</tbody>
</table>

Table 1: Design requirements ranked in rough order of importance.
## Specifications

<table>
<thead>
<tr>
<th>Description</th>
<th>Value</th>
<th>Method of Evaluation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter of reflective membrane.</td>
<td>4 [ft.]</td>
<td>Measure with measuring tape.</td>
</tr>
<tr>
<td>Must weigh less than certain number.</td>
<td>15 [lbs.]</td>
<td>Place on scale.</td>
</tr>
<tr>
<td>Manufacturing budget.</td>
<td>100 [USD]</td>
<td>Evaluate the bill of materials.</td>
</tr>
<tr>
<td>Prototype budget.</td>
<td>500 [USD]</td>
<td>Evaluate the bill of materials.</td>
</tr>
<tr>
<td>Total power output needs to exceed a certain value when testing.</td>
<td>Professor Knox’s Value</td>
<td>Focus light through 2 parallel plates. The front will contain a 2-inch diameter hole that we will shine the light through. This plate will act as a barrier for stray light. The next plate (aluminum) will be imaged with a thermal camera to determine power output.</td>
</tr>
</tbody>
</table>

Table 2: Required design parameters
Optical Design Analysis

Optical Efficiency Analysis

Through our analysis the membrane deforms into a shape that is nearly (3% RMS deviation) parabolic. Optical inefficiencies are introduced by

1. Wrinkles about the edge which scatter light away from the focus.
2. Non uniform pre-tensioning, resulting in axial variations in curvature.
3. Near-Parabolic shape resulting from boundary conditions and load.

Figure 3 & 4: (Left) Knox’s concentrator has a ~1m maximum extent of light distribution, a sign of low efficiency. (Right) Ideal light distribution (~0.3m) from a near-parabolic concentrator, with spot size ~0.1m.

Figure 5 & 6: (Left) Careful measurements of Knox’s concentrator confirm that the shape is within 3% RMS of a parabola. (Right) Finite element models of the membrane are also verified by the measured shape.
Figure 7: Spot size analysis from LightTools on-axis raytrace of the measured membrane shape of Knox’s concentrator. The measured membrane does not include the extremely wrinkled edges, but as shown by the asymmetry of the spot, the membrane is aberrated on-axis which indicates it’s not perfectly parabolic. The size of this spot is 100mm by 60mm, which is similar in size to that of a paraboloid. This is further confirmation that the wrinkles over 7.3% of the aperture in Knox’s prototype are a cause of power loss.

**Reflectance Analysis (Photon Budget)**

Mylar reflectance analysis was conducted utilizing a red laser pointer and a power meter. % Reflectance is a ratio between reflected optical power and incident optical power.

<table>
<thead>
<tr>
<th>Exterior % Reflectance</th>
<th>Interior % Reflectance</th>
</tr>
</thead>
<tbody>
<tr>
<td>77.94</td>
<td>90.34</td>
</tr>
</tbody>
</table>

Table 3: Mylar reflectance on each side measured at 633 nm.

**Solution to Knox Concentrator Optical Inefficiencies**

A driving factor in this project is to maximize the optical efficiency from a solar concentrator. It is known that the Knox concentrator is far from the ideal solar concentrator; however, it has been our job to determine the root of this problem. Throughout this academic year our team has developed a
hypothesis that the optical inefficiencies of the Knox Concentrator is due to non-uniform boundary conditions connecting the mylar membrane to the concentrator frame. The non-uniform boundary condition creates “wrinkles” in the perimeter of the optical surface, which extremely reduce the optical performance of the system.

We sought to prove this hypothesis by conducting surface profile measurements described in Appendix C. This experiment calls for the translation of a laser pointer across the concentrator surface and the reflected beam is marked on a whiteboard across from the concentrator. From these results we can extrapolate sag data (thus describing the profile of our optical surface) and also conduct a primitive experimental “raytrace.” If the membrane at a point is too aberrated, the reflected beam will wildly deviate from its theoretical path, which can be seen as we mark our reflected beam on a white board.

When conducting these measurements on the Knox concentrator and the Senior Design concentrator, the following was determined:

- The Knox concentrator was so aberrated that only 77% of the optical surface could be consistently traced
- The Senior Design concentrator was extremely close to the ideal, and 100% of the optical surface could be consistently traced

These results can be seen in the image below. The black dots represent Senior Design raytrace, while the red dots represent the Knox raytrace. As can be seen below, the black dots from the Senior Design concentrator are quite consistent across the entire optical surface, while the red dots from the Knox concentrator are extremely inconsistent at the edges. Near the edge of the Knox concentrator, wrinkles were extreme, causing such large beam deviation that measurements were impossible to record.

Figure 8: Black Dots: Senior Design concentrator raytrace, Red Dots: Knox concentrator raytrace.
Figure 9: Representative beam deviation experienced at the edge of the Knox concentrator.

Figure 10: Image of Knox concentrator. Note the extreme wrinkles near the edge of the optical surface.
Mechanical Frame Concepts

We chose to approach the frame design problem in many different ways. After generating several frame ideas, the top three concepts were compared for optimality in a Pugh selection matrix, a method which facilitates objective comparison.

Figure 11: On top left, design 1 is the original frame design created by Professor Wayne Knox. Design is a wooden box with an attachment that will create the vacuum. On top right, design 2 is a modular frame design, which can be assembled similar to Ikea furniture but the Mylar is permanently attached to the metal sheeting. The Spider frame mechanism allows for a strong frame support. Metal sheeting will be used for the actual frame. On bottom left, the Final Design is a lightweight design which tensions Mylar evenly. Design is similar to that of a drum head using clamps on the side to provide sealing. On bottom right, a mechanical sealing method for maintaining a vacuum. Rubber tubing will be attached to the lock ring and frame.
Concept Selection Matrix

<table>
<thead>
<tr>
<th>Criteria</th>
<th>Description “Will the design…”</th>
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</thead>
<tbody>
<tr>
<td>Weight</td>
<td>Obtain the minimum weight necessary based on material selection?</td>
</tr>
<tr>
<td>Cost</td>
<td>Obtain the minimum manufacturing/prototype cost based on material selection?</td>
</tr>
<tr>
<td>Sealing Method</td>
<td>Have a method of making an air-tight seal for the vacuum? A passive vacuum is possible but an air-tight seal is ideal.</td>
</tr>
<tr>
<td>Ease of Assembly</td>
<td>Does the prototype take a short time to build, and are we capable of making it with the resources we have?</td>
</tr>
<tr>
<td>Efficiency</td>
<td>Create the optimum total concentrated power, reducing imperfections that may reduce the power output?</td>
</tr>
</tbody>
</table>

Table 4: Pugh selection matrix criteria.

<table>
<thead>
<tr>
<th>Design</th>
<th>Weight</th>
<th>Cost</th>
<th>Sealing Method</th>
<th>Ease of Assembly</th>
<th>Efficiency</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>4</td>
</tr>
</tbody>
</table>

Table 5: Pugh selection matrix results.

From an analysis of the Pugh matrix with certain criteria selection the best design would be design 3 as shown in Figure 10, bottom left.
The Final Frame Design

The frame design used in the final prototype was the ‘Drum-style’ design shown above with a few minor adaptations. Unforeseen complications arose when using the rubber tubing on both the top ring and the main base. Due to the nature and shape of the tubing, when the sealing pressure was applied, the rubber would misalign and cause large creases to form in the mylar. To prevent this problem, the top ring was flipped, leaving the flat side to create the necessary seal against one ring of rubber tubing.

![Frame CAD](image)

Figure 12: The frame was machined using a 10ft X 10ft CNC router (right) located on the first floor of Rettner Hall. The wood chosen for the frame is a high-quality Russian Birch Plywood because of its strength and density, giving the vacuum minimal leakage when applied to the concentrator while also maintaining great stability.

Currently, our frame consists of the circular base, a top ring to lock the mylar in place, rubber tubing to create and even seal around the mylar, and eight C-clamps arranged to evenly distribute tension around the perimeter of the concentrator.

Frame CAD for Fabrication

The selected frame design could be manufactured in the following ways:

1. Cut the entire frame as a single piece on a large CNC router
2. Cut segments of frame on a small CNC router
3. Cut the entire frame as a single piece using a handheld jigsaw
4. Cut the entire frame as a single piece using a handheld router

We have decided to manufacture our frame using method (1) because cutting the frame as a single piece ensures that the boundary conditions are circularly symmetric.
Figure 13: Bottom ring (47” OD, 44” ID, 2” depth) after manufacture on large CNC router and assembly with wood glue. This ring is comprised of two thinner rings, each of 1” depth. The rings are made of high-quality Russian birch plywood.

Figure 14: Rubber gasket, embedded into the frame.
Optical Testing Results

This section outlines results relating to optical performance for both Senior Design and Knox concentrators. Relative power, maximum temperature, and spot size is analyzed. The results below show definitively that the Senior Design concentrator outperforms the Knox concentrator.

Relative Power

During testing described in Appendix D, both concentrators were imaged onto a metal plate 10 feet away. A point and shoot temperature readout device was utilize to record temperature on the plate over the span of one minute. Since temperature rate over time is proportional to optical power, the slope of this data will yield relative power. The metal plate radiates as a blackbody, and at some point in time the rate of energy lost to blackbody radiation equals the rate of energy absorbed from the solar concentrator. When plotting the temperature against time, this looks like the temperature flattens out or plateaus. Therefore, when monitoring only the temperature of the plate, the power will be most accurately calculated by fitting a trend line through the beginning of the data. In our analysis, the first minute of recorded data was fit to obtain power values. Results are shown below:
Figure 16: Senior Design and Knox concentrator temperature (deg F) vs. time (s), which yields a slope indicative of relative power.

- Knox’s concentrator: **0.86 degrees Fahrenheit per second**
- Senior Design Team’s concentrator: **1.29 degrees Fahrenheit per second**

Since the temperature rate with time is proportional to the optical power, it is concluded that the senior design team’s concentrator yields a power that is **50% greater than Professor Knox’s concentrator**.

**Maximum recorded temperature**

Another indicator of optical performance is maximum recorded temperature. The maximum temperature recorded from the point and shoot device may not necessarily be the maximum temperature of the entire plate. However, the thermal imaging camera captures the temperature of the entire plate throughout testing. Thus, we can compare maximum temperature readouts for both Senior Design and Knox concentrator.

The metal plate was recorded with a thermal camera during testing of Senior Design and Knox concentrators. The maximum temperature recorded for each was as follows:
Figure 17: Senior Design and Knox concentrator maximum temperature readings.

- Knox’s concentrator: **43 degrees Celsius, or 109 degrees Fahrenheit**
- Senior Design Team’s concentrator: **229 degrees Celsius, or 444 degrees Fahrenheit**

### Spot Size

Another extremely important indicator of optical performance is spot size. Ideally, maximum performance would be obtained when the spot size is as small as possible. The ideal shape is a small circular spot. The Knox concentrator produces a spot that is extremely aberrated, while the Senior Design concentrator produces a spot that is extremely compact and circular in nature. The focused spots are shown below:

Figure 18: Left: Knox concentrator focused spot. Right: Senior Design concentrator focused spot. It can be noted that the Knox concentrator spot is extremely aberrated compared to the Senior Design concentrator spot.
## Cost Analysis

<table>
<thead>
<tr>
<th>Materials</th>
<th>Quantity</th>
<th>Part Price</th>
<th>Unit Price (Final Design)</th>
<th>Unit Price (Mass-Manufacturing)</th>
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<tr>
<td>1&quot;x48&quot;x96&quot; Apple Plywood Sheet</td>
<td>2</td>
<td>$160.00</td>
<td>$320.00</td>
<td>$90.00</td>
</tr>
<tr>
<td>Silicone</td>
<td></td>
<td>10.1 oz. White Window and Door Caulk</td>
<td>1</td>
<td>$5.92</td>
</tr>
<tr>
<td>Titebond</td>
<td></td>
<td>16 oz. Premium Wood Glue</td>
<td>1</td>
<td>$5.47</td>
</tr>
<tr>
<td>1/4&quot; x 0.170&quot; x 20' PVC Tubing</td>
<td>1</td>
<td>$3.25</td>
<td>$3.25</td>
<td>$0.48</td>
</tr>
<tr>
<td>1/8&quot; x 4' x 8' Utility Panel</td>
<td>1</td>
<td>$9.96</td>
<td>$9.96</td>
<td>$4.98</td>
</tr>
<tr>
<td>2&quot; x 54&quot; x 25' roll Sunfilm Mylar Film Roll</td>
<td>1</td>
<td>$22.70</td>
<td>$22.70</td>
<td>$4.54</td>
</tr>
<tr>
<td>4&quot; Industrial C-Clamp</td>
<td>10</td>
<td>$3.99</td>
<td>$39.90</td>
<td>$0.00</td>
</tr>
<tr>
<td>1/4-20 Threaded 2' Rod</td>
<td>4</td>
<td>$1.47</td>
<td>$5.88</td>
<td>$5.88</td>
</tr>
<tr>
<td>1/8&quot;x1.5&quot;x96&quot; Aluminum Flat Bar</td>
<td>1</td>
<td>$21.89</td>
<td>$21.89</td>
<td>$21.89</td>
</tr>
<tr>
<td>1/4 size, Zinc-Plated Hex Nut</td>
<td>16 (100 per box)</td>
<td>$5.37/b ox</td>
<td>$5.37</td>
<td>$0.86</td>
</tr>
<tr>
<td>High-Temperature Silicon Cord</td>
<td>50'</td>
<td>$6.88/ft</td>
<td>$344.00</td>
<td>$86.00</td>
</tr>
<tr>
<td><strong>TOTAL COST</strong></td>
<td>N/A</td>
<td>N/A</td>
<td><strong>$784.34</strong></td>
<td><strong>$226.47</strong></td>
</tr>
</tbody>
</table>

Table 6: Bill of materials for final design materials and manufacturing. Manufacturing costs are an estimated reduced price if the concentrators are produced in bulk-- each value is reduced by a factor of 5.
Weight Analysis

Both the Senior Design and Knox concentrators were weighed to evaluate system mass. The results were as follows:

<table>
<thead>
<tr>
<th>Senior Design Concentrator Weight (lbs.)</th>
<th>Knox Concentrator Weight (lbs.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>34.4</td>
<td>43.0</td>
</tr>
</tbody>
</table>

Table 7: Design comparison table for weight.

From these results it is apparent that our design did not meet the intended 15 pound weight specification. However, much of this weight comes from the use of industrial c-clamps, which were last minute additions to the design. Future iterations of this project could easily implement a less massive solution by replacing the c-clamps. In addition, it is important to note that the Senior Design concentrator is 8.6 pounds lighter than the Knox concentrator.
Appendix A: Optical System Design

Overview:

We seek to create a series of optical models LightTools. The first will be of a mirror fit to the Hencky Curve, an equation that theoretically describes our in use membrane shape. The second will be an accurate representation of our final solar concentrator. The third will be an accurate representation of Wayne Knox’s solar concentrator. Radiometric analysis will be run on all models in order to compare models, establish theoretical thresholds, and estimate negative performance impacts.

Theoretical Membrane (Hencky Curve) Model:

We seek to model the theoretical shape of our mirror, which is neither spherical nor parabolic. The actual shape follows the Hencky Curve. The Hencky Curve is the shape that results from a uniform, circular boundary condition that is acted upon by a uniform pressure. We utilize an equation for sag \( z \) that approximates the Hencky Curve:

\[
z(u) = \frac{D}{64F^2}(u^2 + 0.111u^4)
\]

Where \( z \) is sag in mm, \( F \) is mirror focal length in mm, and \( u \) is axial displacement from the origin in mm. Using this equation, we first need to model the curve in MATLAB:

Next, we create a 3D mesh in MATLAB representing our Hencky Curve surface. From here, we can take the 3D mesh data from MATLAB and translate it into a freeform reflective surface in LightTools by manual transfer of the data points:
With the LightTools Hencky Curve Model, we can run radiometric analysis for our theoretical membrane shape. We will compare these results to both Wayne Knox’s and our own solar concentrators.

**Actual Membrane Models:**

Using data collection methods defined in the Test Plan section, we gather 3D mesh data that describes the shape of the membrane. From here we can manually enter this data into LightTools as a freeform reflective surface:
Fill Factor Loss:

We considered two possible methods for scaling the design:

- Array of 19 1ft diameter mirrors aligned to common focus
  - Smaller mirror apertures means smaller spherical aberration contribution
  - Tipped mirrors introduces coma
  - Loss from fill factor

- Single 4ft diameter reflecting Mylar membrane, 10ft focal length
  - More spherical aberration due to larger aperture
  - Zero fill factor loss

These two methods were tested in Lighttools. The single mirror design outperforms the array design by an order of magnitude.
Appendix B: Finite Element Modeling

Summary of model:

- Material: 0.006” thick Mylar membrane, material properties from matweb.com
- Boundary conditions: Fixed translation on 4ft diameter rim
- Load: Uniform pressure of 0.1psi normal to surface
- Displacement output from model: FEA shape is within 1.5% of parabolic shape

Conclusions:

- The non-parabolic shape of WHK prototype shape is not caused by load conditions modeled.
- Non-uniformities are caused by:
  
  o Non-uniform tensioning of membrane. Membrane must be evenly tensioned for circularly symmetric shape. Due to lack of control in tensioning process, different axes have different curvatures. This results in astigmatism which blurs the spot.

  o Non-uniformities in boundary conditions. If the frame is not circular, the membrane under load will not be symmetric.
- The frame design must mitigate the issues of non-uniform tension and boundary.
Appendix C: Surface Profile Test Plan / Validation

In order to validate the ideal FEA parabola to be within 1.5% of a perfect parabola, a testing method capable of 0.5mm resolution is required. We are investigating the implementation of a laser displacement measurement.

Surface Testing and Model Validation:

A HeNe laser pointer will be used to measure the displacement caused from a known position. A laser pointer is placed upon an optical rail and directed upon the concentrator. The spot is then marked upon the whiteboard and the laser pointer is then translated to a fixed increment away upon the rail. The spot is then marked and the process is repeated. After the entire concentrator is scanned (without any major blur in the spot present), the displacement from the “zeroth” spot is measured with a fixed ruler.

The purpose of this measurement is two-fold:

- To input surface profile into LightTools and validate spot shape against picture of WHK prototype spot shape
- To compare measured surface profile against FEA surface profile for model validation
Illustrative Results:

The above graph shows the measured deflection of the laser spot, as the laser was translated across the optical rail. Due to the hand measurements taken and subsequent calculations, error bars are set at ± 0.5 mm.

The above picture illustrates the sag profile measurement conducted using the laser displacement test. It is notable that this curve is parabolic to within 3%. Deviations from the parabolic are large in the center, where the curve is flatter. It is also notable that we were unable to measure the extremes of the curve due to wrinkles on the membrane → this profile represents 77% of the membrane.
Appendix D: Optical Performance Test Plan

In order to compare performance of the senior design teams product to that of professor Knox, a testing method was devised that yields data proportional to that of power. This testing method serves as a final validation that our product outperforms that of professor Knox.

**Optical Test Setup:**

The concentrator is angled to capture sunlight such that its imaging spot is located on the center of an elevated metal plate located 10 feet away from the base of the concentrator. Variable vacuum pressure is utilized to change concentrator focal length and make the image spot size of the concentrator as small as possible on the metal plate. A thermal imaging (FLIR) camera, positioned to capture the entire metal plate, is utilized to take thermal images of the metal plate over a duration of five minutes. Temperature is also recorded utilizing a point-and-shoot temperature readout device. This test is conducted for both senior design and Knox products.
Left: Image of test setup being assembled. Right: close up of spot being focused onto The concentrator is positioned 10 feet away from a metal test plate. Vacuum will be applied to the concentrator to focus sunlight onto the metal plate. Thermal images will be recorded with both a point and shoot temperature readout device (pictured on the left and right) and an IR thermal camera (pictured on the right). Note that in the final setup, the metal plate with a hole was removed as it was too difficult to focus the beam through the hole.